

## Relational Typed Set Calculus

A set is a collection of distinct objects, a typed set classifies the membership of the set in meta-math.

### Example

Three dimensional space is defined by a collection of points on three axis: x, y and z. In our definition of space x, y and z must be real numbers. In this theory the number of points in subsets of typed sets must be the same in order for them to be valid, as x y and z are treated independently but correlated.

Space is further defined by a second-order meta-description that defines the total dimensional distance, relative to the pole (0, 0, 0).

$$\begin{aligned} \widehat{space} &:= \left[ \begin{array}{c} \langle \langle x \rangle : R^+, \langle y \rangle : R^+, \langle z \rangle : R^+ \rangle \\ \vdots \\ \sqrt{x^2 + y^2} + \sqrt{x^2 + z^2} + \sqrt{y^2 + z^2} \end{array} \right] \triangleq \widehat{\mathfrak{S}} \\ \mu \widehat{\mathfrak{S}} &= \langle \sqrt{x^2 + y^2} + \sqrt{x^2 + z^2} + \sqrt{y^2 + z^2} \rangle \\ \partial^x \widehat{\mathfrak{S}} &= \langle \sqrt{x^2 + y^2} + \sqrt{x^2 + z^2} \rangle \\ \partial^y \widehat{\mathfrak{S}} &= \langle \sqrt{x^2 + y^2} + \sqrt{y^2 + z^2} \rangle \\ \partial^z \widehat{\mathfrak{S}} &= \langle \sqrt{x^2 + z^2} + \sqrt{y^2 + z^2} \rangle \\ \widehat{\mathfrak{S}}^n \cap \widehat{\mathfrak{S}}^m &= \langle \langle n_x \mid \partial^x \leq \partial^x \widehat{\mathfrak{S}}^m \wedge \leq m_x \wedge \mu \leq \mu m \cup m_x \mid \partial^x \leq \partial^x \widehat{\mathfrak{S}}^n \wedge \leq n_x \wedge \mu \leq \mu n \rangle, \\ &\langle \langle n_y \mid \partial^y \leq \partial^y \widehat{\mathfrak{S}}^m \wedge \leq m_y \wedge \mu \leq \mu m \cup m_y \mid \partial^y \leq \partial^y \widehat{\mathfrak{S}}^n \wedge \leq n_y \wedge \mu \leq \mu n \rangle, \\ &\langle \langle n_z \mid \partial^z \leq \partial^z \widehat{\mathfrak{S}}^m \wedge \leq m_z \wedge \mu \leq \mu m \cup m_z \mid \partial^z \leq \partial^z \widehat{\mathfrak{S}}^n \wedge \leq n_z \wedge \mu \leq \mu n \rangle \rangle \\ \partial \partial^x \widehat{\mathfrak{S}} &= \langle \langle x \mid \partial^x \geq \partial^x(\widehat{\mathfrak{S}} - n) \wedge (\partial^y \geq \partial^y(\widehat{\mathfrak{S}} - n) \vee \partial^z \geq \partial^z(\widehat{\mathfrak{S}} - n)) \rangle \rangle \\ \partial \partial^y \widehat{\mathfrak{S}} &= \langle \langle y \mid \partial^y \geq \partial^y(\widehat{\mathfrak{S}} - n) \wedge (\partial^x \geq \partial^x(\widehat{\mathfrak{S}} - n) \vee \partial^z \geq \partial^z(\widehat{\mathfrak{S}} - n)) \rangle \rangle \\ \partial \partial^z \widehat{\mathfrak{S}} &= \langle \langle z \mid \partial^z \geq \partial^z(\widehat{\mathfrak{S}} - n) \wedge (\partial^x \geq \partial^x(\widehat{\mathfrak{S}} - n) \vee \partial^y \geq \partial^y(\widehat{\mathfrak{S}} - n)) \rangle \rangle \\ \oint \widehat{\mathfrak{S}} &= \langle \langle x \mid \in \partial \partial^x \rangle, \langle y \mid \in \partial \partial^y \rangle, \langle z \mid \in \partial \partial^z \rangle \rangle \\ \text{Area of space} &\triangleq \dot{s} = \sum \mu \oint \widehat{\mathfrak{S}} \end{aligned}$$

thought

$$\begin{aligned} & \left[ \begin{array}{c} \langle \langle utility_{real} \triangleq u_r \rangle : R^+, \langle utility_{imaginary} \triangleq u_i \rangle : R^+ \rangle \\ \vdots \\ \left| \left( coefficient_{real_n}(u_r) + coefficient_{imaginary_n}(u_i) \triangleq (coefficient_{marketplace_n})(t_{n\infty}) \right) \right| \\ coefficient_{real_n} + coefficient_{imaginary_n} = 1 \end{array} \right] \\ & \triangleq \widehat{\mathfrak{I}} \end{aligned}$$

